

# Fast prediction method for approximating steady flow simulations over multiple domains

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# h3-Open-DDA in h3-Open-BDEC

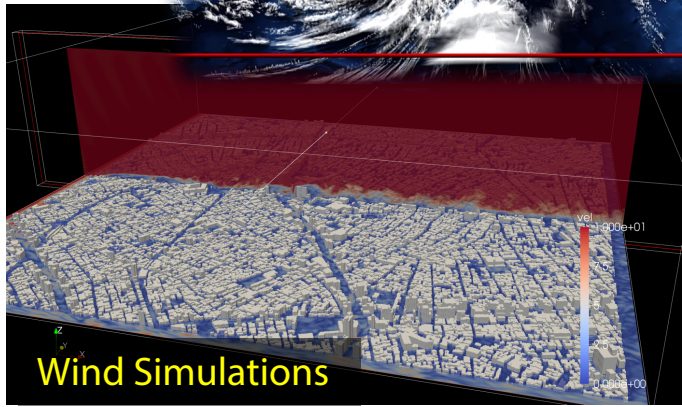
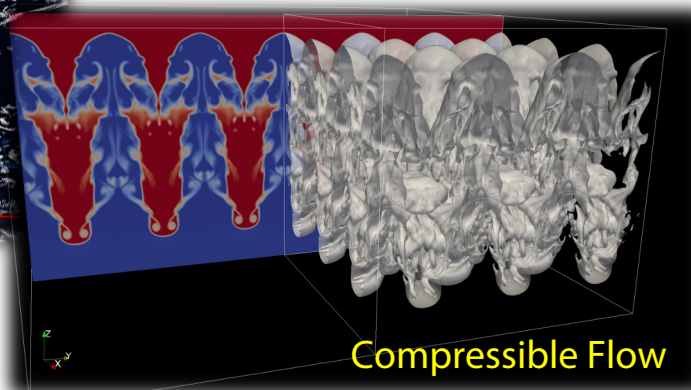
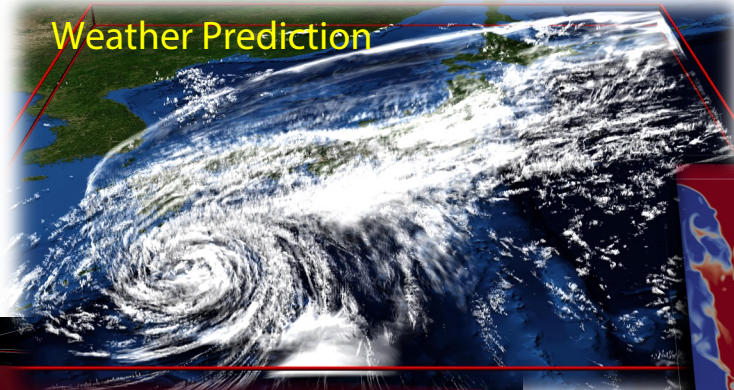
## ■h3-Open-DDA

- Data Driven Approach (DDA)
  - Integration of simulation and machine learning
- Hierarchical DDA (hDDA)
  - Training data generation and learning in efficient and realistic time by simple model
  - Reducing computation time, computation volume, and power consumption (less than 1/10 of conventional methods)

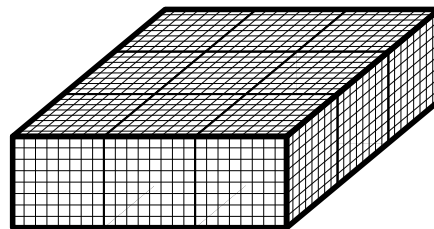
## ■Research topics

- Prediction of steady-state flow over multiple domains by combining deep learning and boundary conditions
- Development of a fast prediction method for time-dependent flows
- Enhancement of molecular dynamics simulation by machine learning

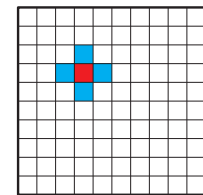
# Target: Computational Fluid Dynamics



Computational cost of computational fluid dynamics is relatively high.



Computational domain



Stencil computations<sup>3</sup>

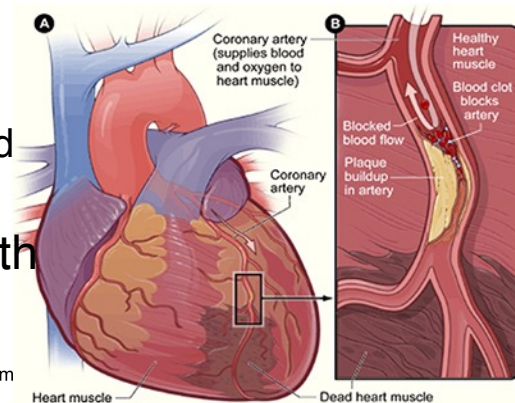
# Goal: Fast Prediction of Blood Flow Simulation

## ■ Background and Motivation

- Recently, computational fluid dynamics (CFD) has been used to compute the blood flow and to diagnose the severity of coronary stenosis.
- However, since CFD requires large computational resources, it is indispensable to accelerate the process of CFD analysis.
- In order to solve this problem, we will use deep learning to build a fast surrogate for approximating the large-scale 3D blood flow simulation.

## ■ Challenge

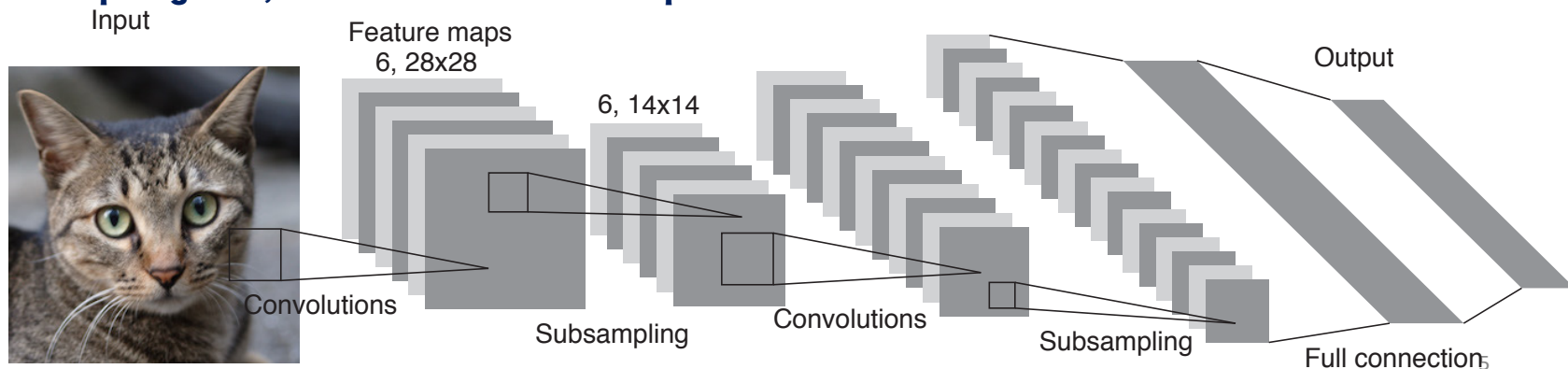
- Developing deep learning surrogate for 2D/3D steady flow
  - Training models on multiple GPUs using PyTorch and Horovod
  - Predicting flow around a complex shape.
- Developing a prediction method using deep learning with boundary exchange for 3D CFD simulation results



Adapted from  
<https://www.drshreshbhagia.com/patient-guide/overview-of-coronary-artery-disease/>

# Deep learning / Convolutional Neural Network

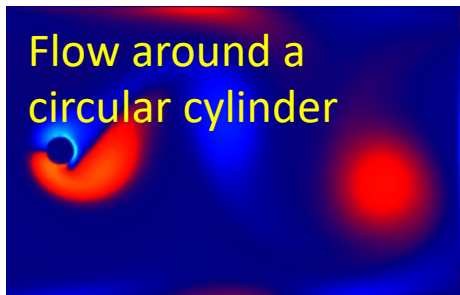
- Deep learning is one of methods of machine learning based on neural networks.
- A deep neural network (DNN) is a neural network with multiple layers between the input and output layers.
- A convolutional neural network (CNN) is one of the representative of DNN.
- CNNs are utilized with great success in image recognition, analysis and classification.
- In our project, we use CNNs to predict the CFD simulations results.



# Fast prediction of CFD simulation results by DNN

## Dataset

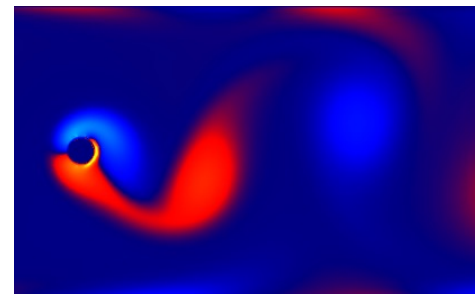
Flow around a circular cylinder



CFD simulation  
(Lattice Boltzmann  
methods)

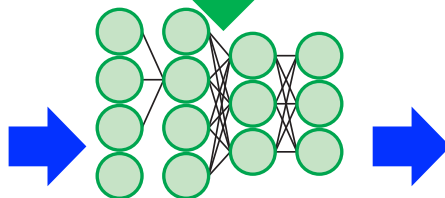
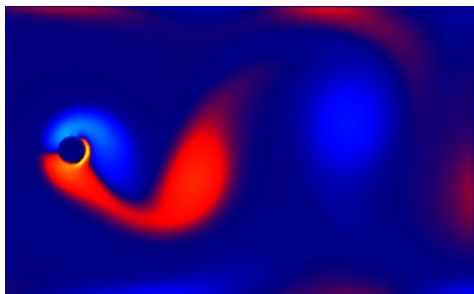


$$f_i(x + c_i \Delta t, t + \Delta t) = f_i(x, t) + \Omega_i(x, t)$$
$$\Omega_i(x, t) = -\frac{1}{\tau} (f_i(x, t) - f_i^{eq}(x, t))$$



## Training

## Prediction



Convolutional neural networks (CNNs) to  
predict simulation results

Prediction of flow

CNNs may become “faster simulator”

# Datasets

## ■ Steady flow

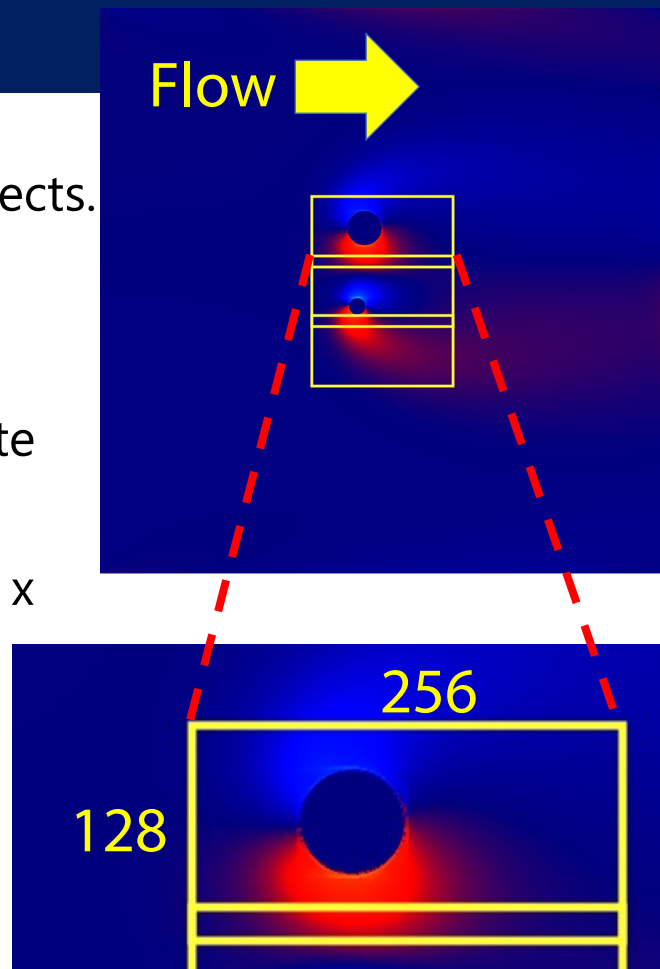
- The fluid flows along the x axis around objects.

## ■ LBM (Lattice Boltzmann method) simulation results

- D2Q9 model (9 variables is used for discrete velocity)
- $Re = 20$ ,
- Region size:  $256 \times 128$  ( clipped from  $1024 \times 1024$ )
- 6 types of object shapes:
  - polygons (number of angles: 3-7)
  - cylinders.

## ■ Input data: $256 \times 128$ (clipped)

- Training: 14515
- Validation: 1613

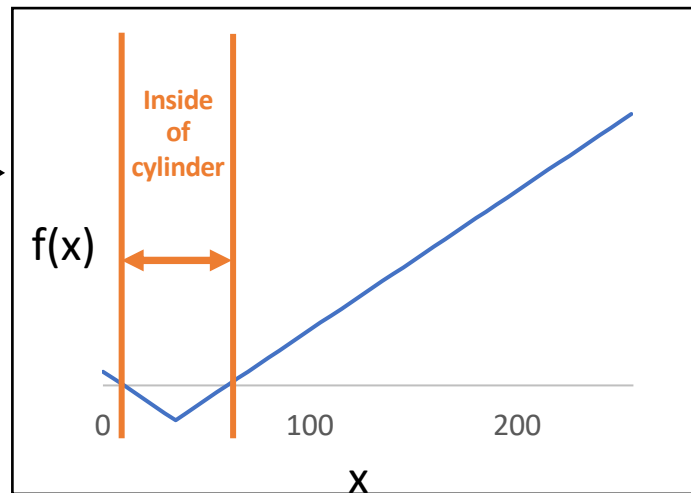
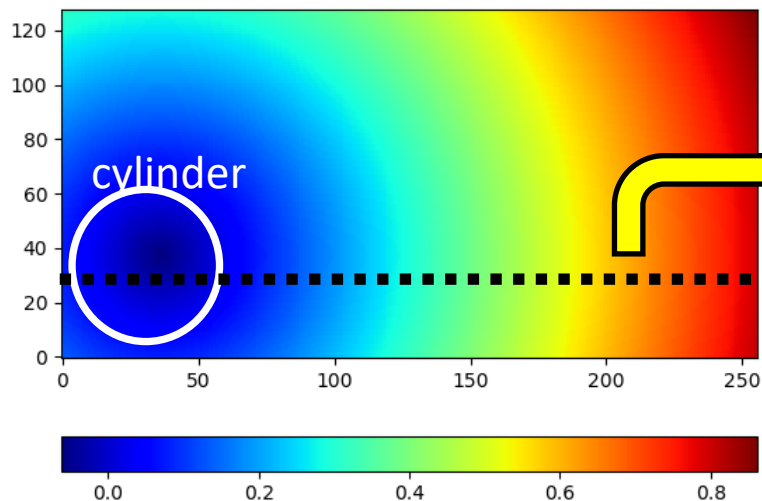


# Singed distance function (SDF)

## ■ SDF represents

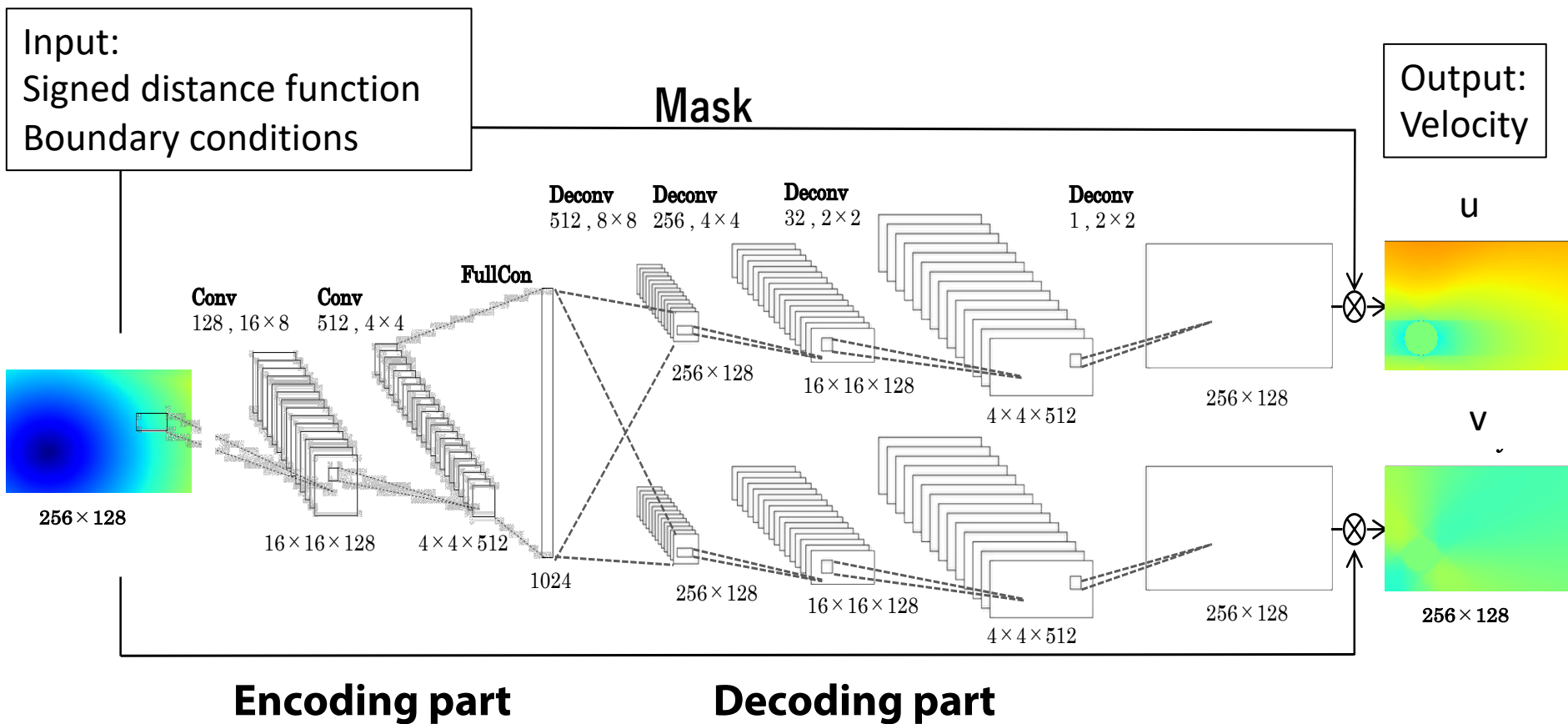
- the surface of the object as zero.
- the outside of the object as a positive distance.
- the inside of the object as a negative distance.

## ■ A universal representation for different geometry shapes and works efficiently with neural networks





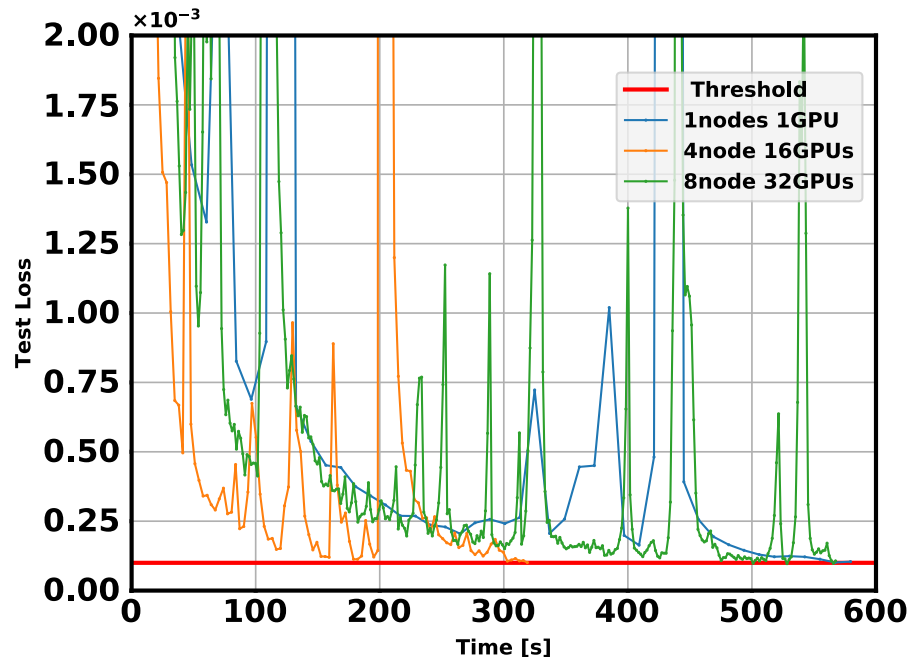
# Network Architecture and Training



# Accelerating training with multiple GPUs

## ■ Implementing models with PyTorch and Horovod

### Learning curves using multiple GPUs on Reedbush-L

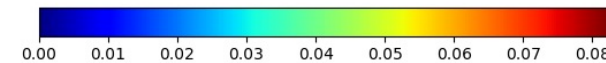
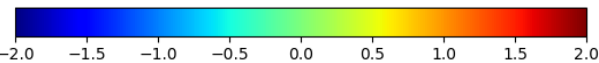
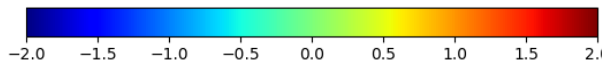
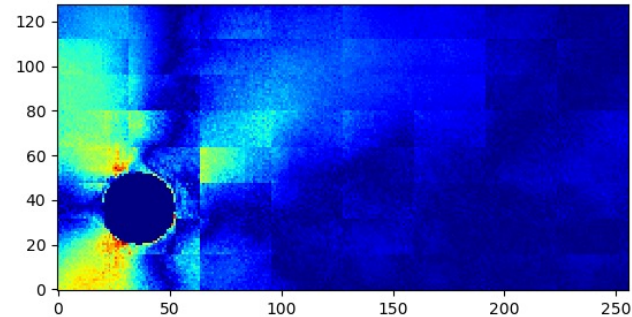
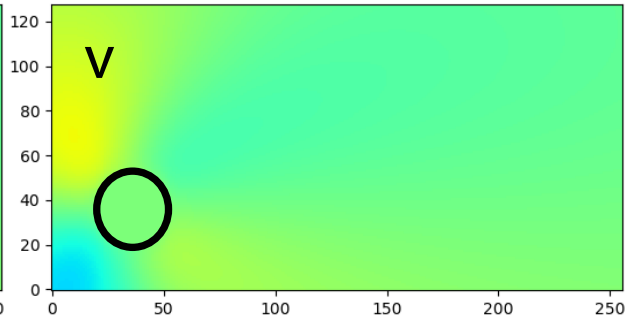
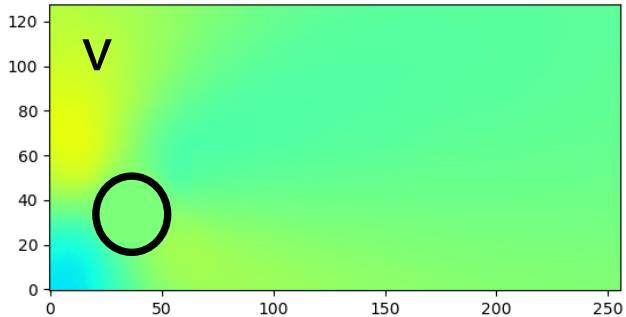
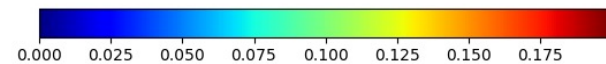
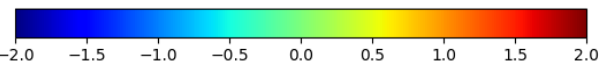
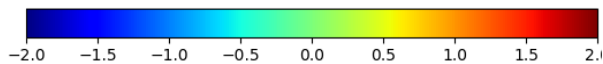
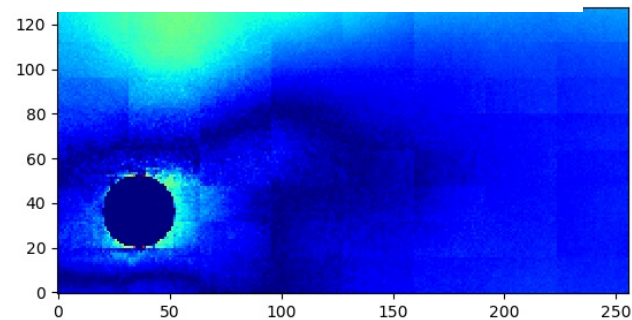
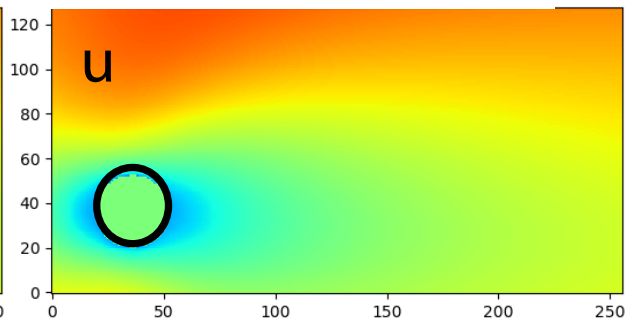
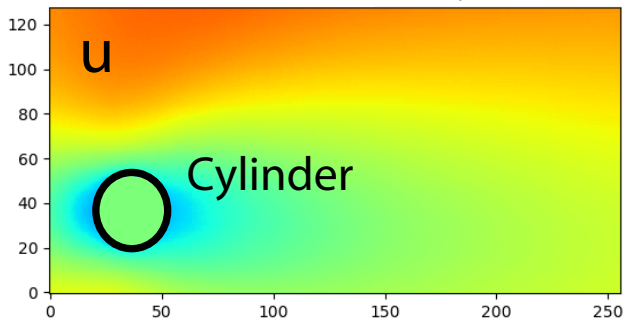


# Prediction results for single domain

CNN Prediction

LBM Ground truth

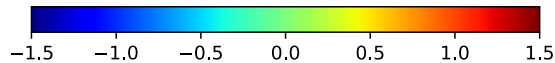
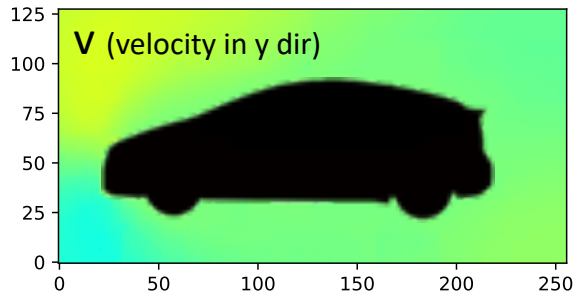
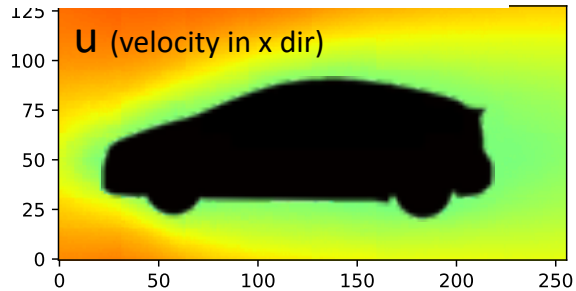
Err = |CNN - LBM|



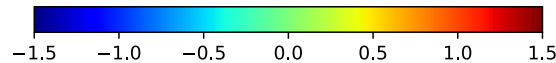
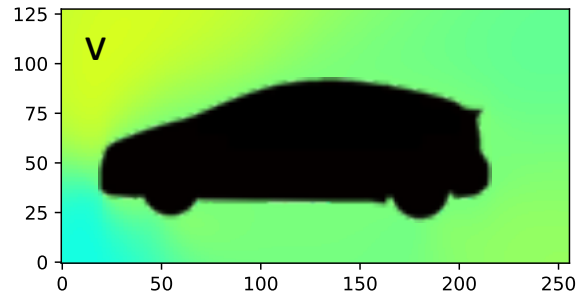
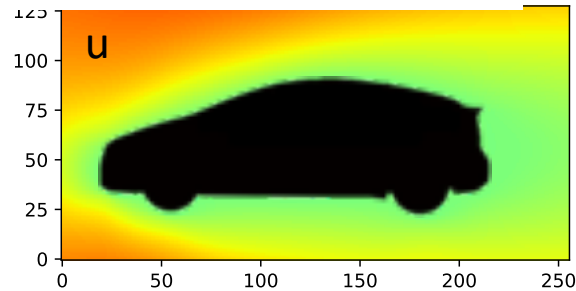
Loss:  $7.3 \times 10^{-5}$

# Prediction results for a complex shape

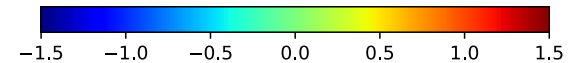
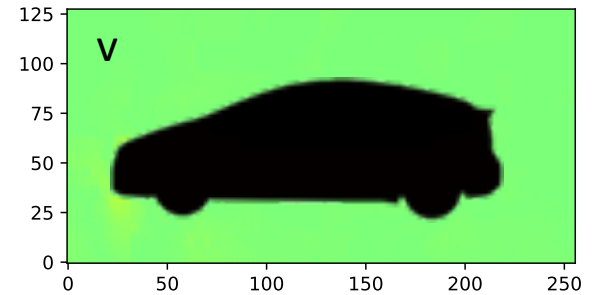
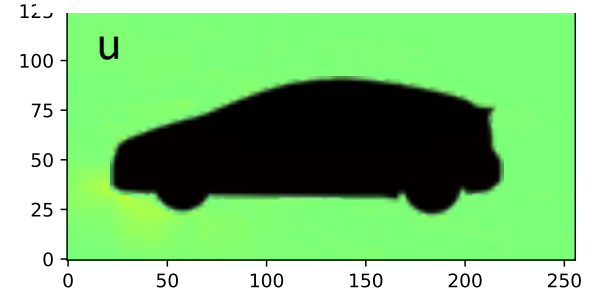
## CNN Prediction



## LBM Ground truth



## Err = |CNN - LBM|

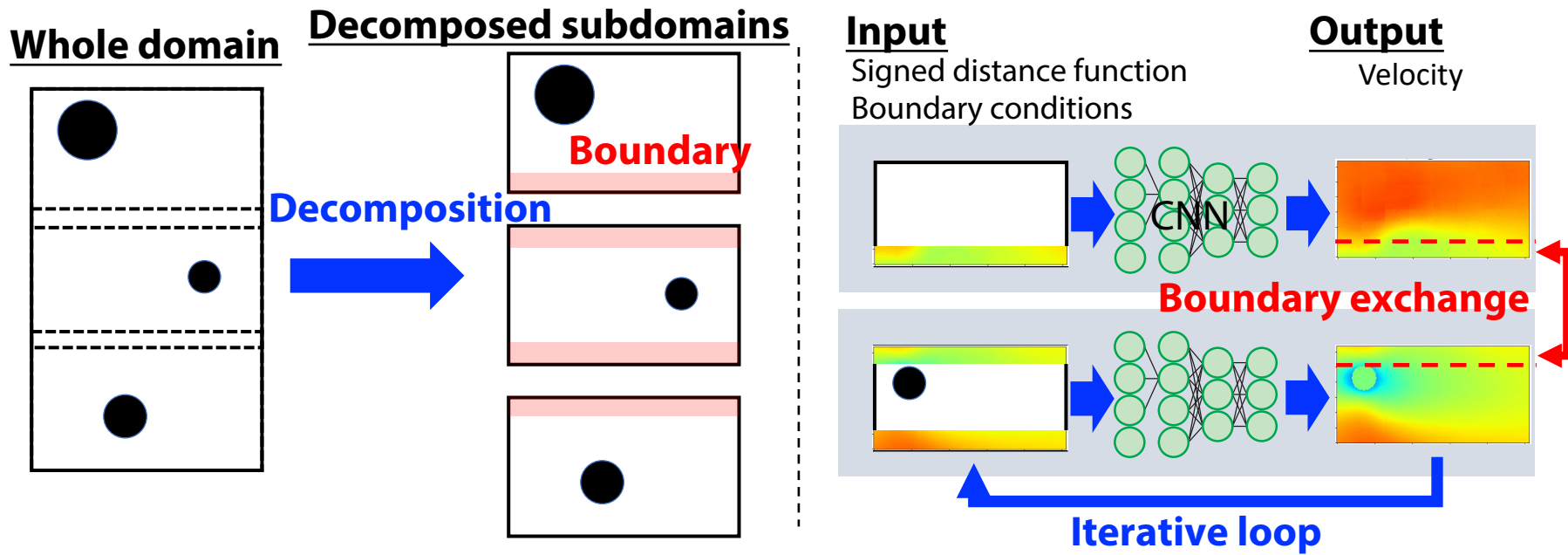


• Computation time... LBM (82,000steps)  $\rightarrow$  41.1 sec 、 CNN prediction  $\rightarrow$  0.6 sec

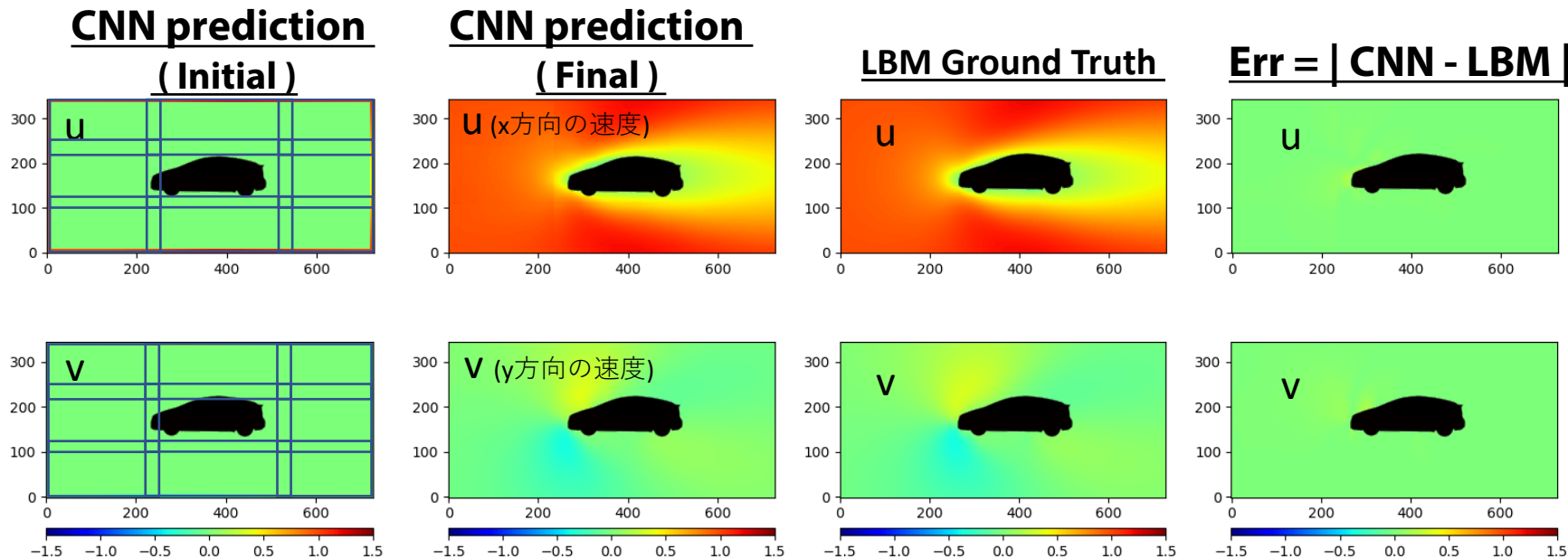
$\Rightarrow$  CNN prediction has achieved high accuracy with significant reduction in calculation time.

# Prediction by CNN with boundary exchange

- The network model trained for a single domain is applied to the decomposed subdomains to predict the simulation results in each subdomain.
- In order to maintain consistency between values in the subdomains, boundary exchange between neighbor subdomains is performed.
- CNN and boundary exchange are performed iteratively until values converge.
- This method has no limitation for device (GPU) capacity.



# Predicted results using CNN with boundary exchange

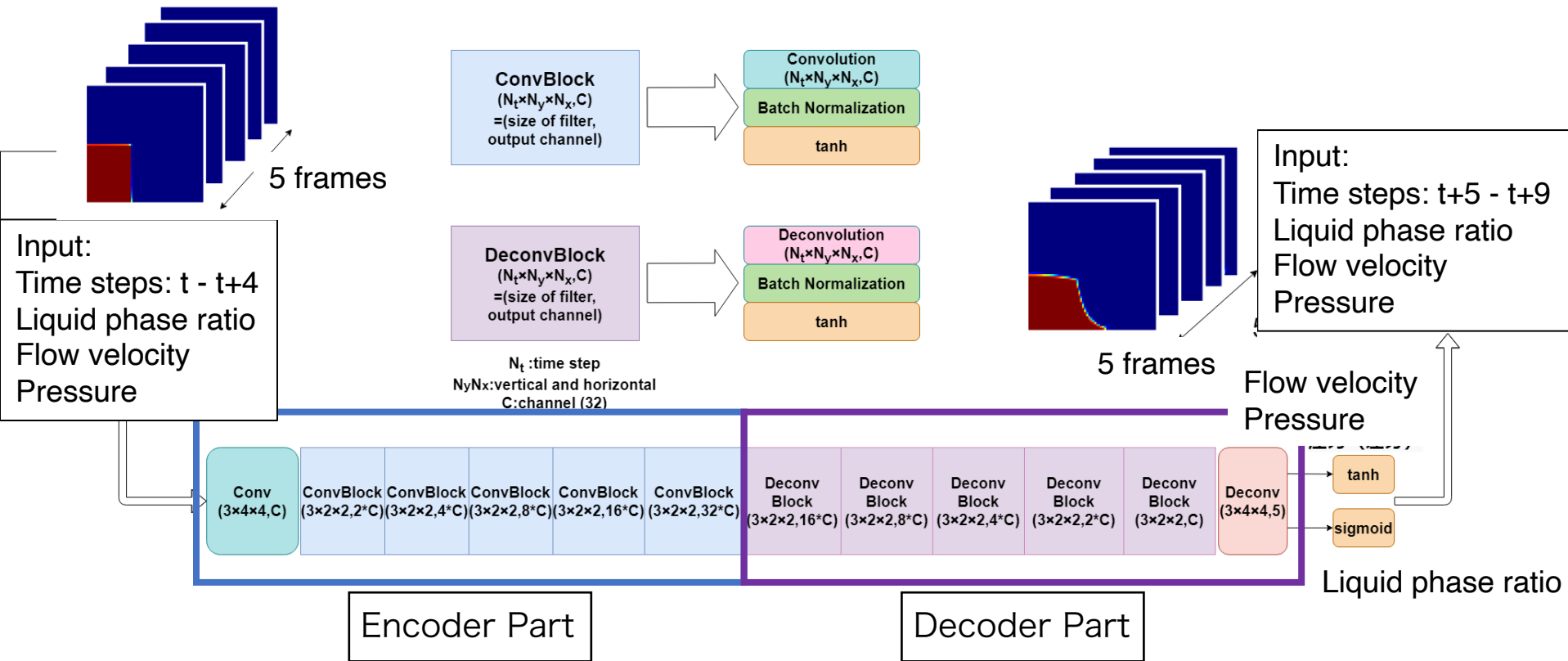


Domain size : 748 x 364 (9 decomposed subdomains)

Mean error : 3.89%

Comp. time : 3.82 s

# Future plan: Extending to Time dependent flow



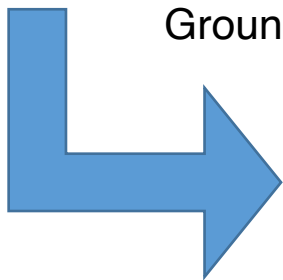
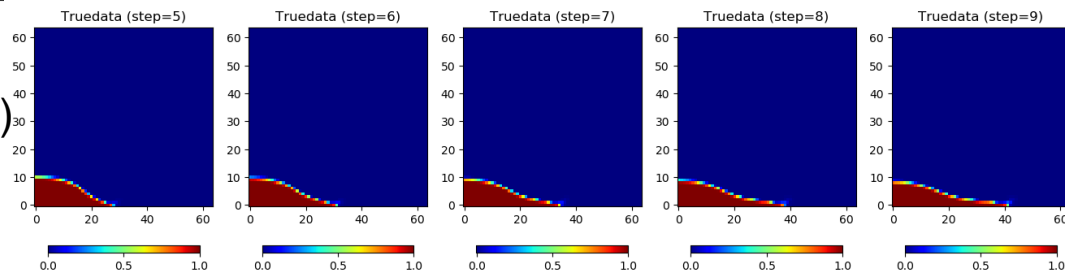
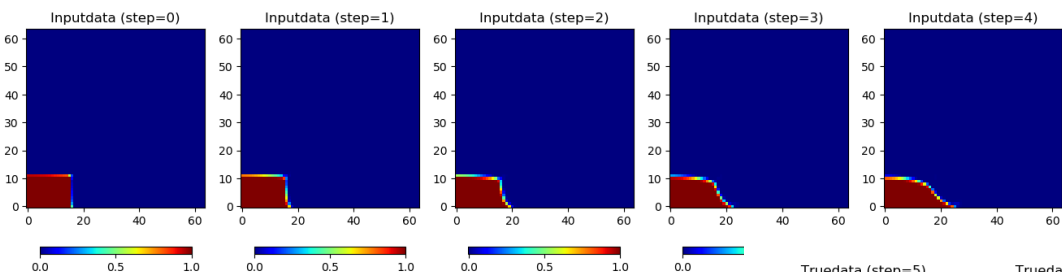
# Prediction (Liquid phase ratio)

Input (5 frames)

Liquid-Phase Ratio

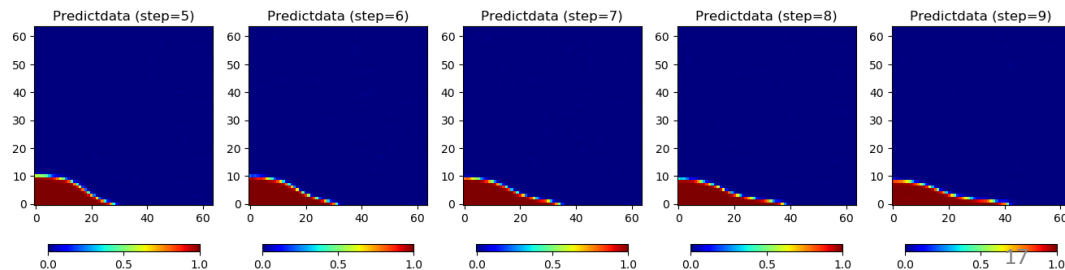
Datasets:

OpenFOAM simulation results (50 cases)



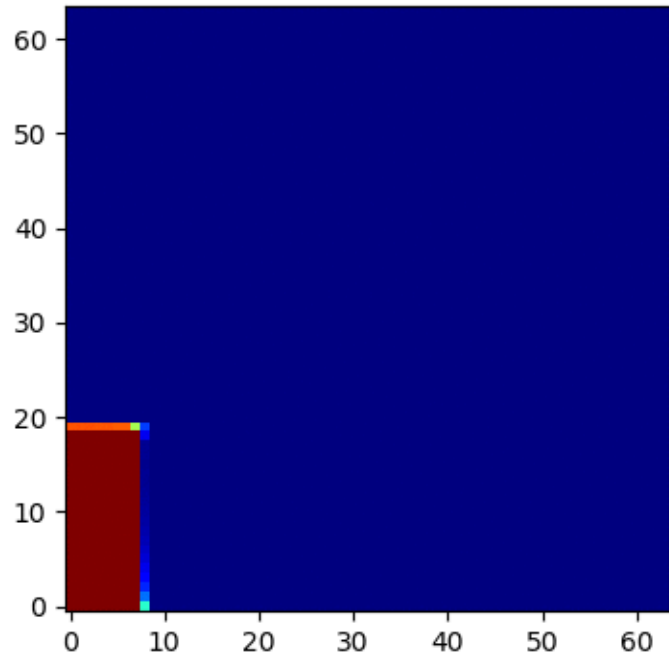
Ground truth (5 frames)

Prediction (5 frames)

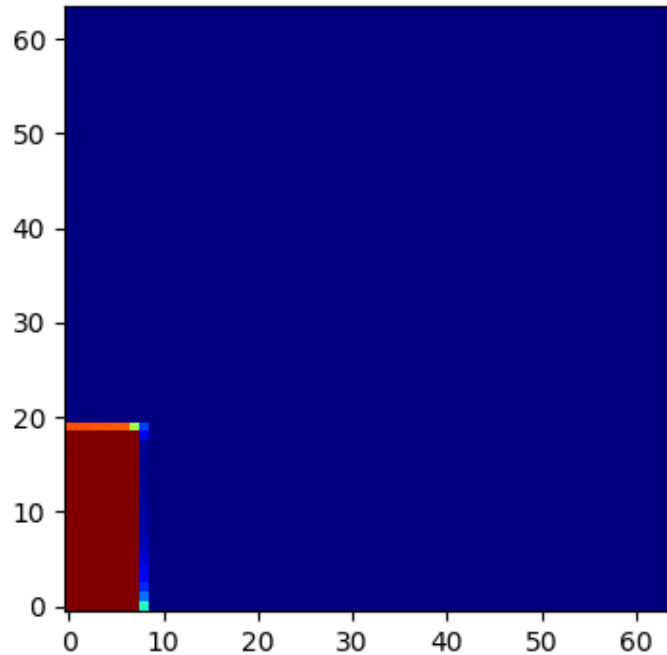




# Prediction result (Liquid phase ratio)



Ground truth (OpenFOAM)



CNN Prediction

# Conclusion

## ■ Deep learning fast surrogate for steady flow

- Predicting the LBM results by using convolutional neural networks (CNNs).
  - Predicting flow around a complex shape.
- Predicting simulation results on large domain using CNNs with boundary exchange.
  - The proposed method has no limitation for device (GPU) capacity.

## ■ Time dependent flow

- Predicting OpenFOAM simulation results using 3D CNN.

## ■ Future works

- We will improve a prediction method for large-scale computational results.
- We will apply the fast surrogate for steady flow to blood simulations.
- We plan to extend our research to the development of fast prediction methods for time dependent flows.